

Section 9.7 Probability

Solutions to Even-Numbered Exercises

2. {2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12}
4. {(red, red), (red, blue), (red, black), (blue, blue), (blue, black)}
6. {SSS, SSF, SFS, FSS, SFF, FFS, FSF, FFF}
8. $E = \{\text{HHH, HHT, HTH, HTT}\}$
- $$P(E) = \frac{n(E)}{n(S)} = \frac{4}{8} = \frac{1}{2}$$
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12. The probability that the card is *not* a face card is the complement of getting a face card. (See Exercise 11.)
- $$P(E') = 1 - P(E) = 1 - \frac{3}{13} = \frac{10}{13}$$
14. There are 8 possible cards in each of 4 suits:
 $8 \cdot 4 = 32$
- $$P(E) = \frac{n(E)}{n(S)} = \frac{32}{52} = \frac{8}{13}$$
16. $E = \{(2, 6), (3, 5), (3, 6), (4, 4), (4, 5), (4, 6), (5, 3), (5, 4), (5, 5), (5, 6), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6)\}$
- $$P(E) = \frac{n(E)}{n(S)} = \frac{15}{36} = \frac{5}{12}$$
18. $E = \{(1, 1), (1, 2), (2, 1), (6, 6)\}$
- $$P(E) = \frac{n(E)}{n(S)} = \frac{4}{36} = \frac{1}{9}$$
20. $E = \{(1, 1), (1, 2), (1, 4), (1, 6), (2, 1), (2, 3), (2, 5), (3, 2), (3, 4), (3, 6), (4, 1), (4, 3), (4, 5), (5, 2), (5, 4), (5, 6), (6, 1), (6, 3), (6, 5)\}$
- $$P(E) = \frac{n(E)}{n(S)} = \frac{19}{36}$$
22. $P(E) = \frac{{}_2C_2}{{}_6C_2} = \frac{1}{15}$
24.
$$P(E) = \frac{{}_1C_1 \cdot {}_2C_1 + {}_1C_1 \cdot {}_3C_1 + {}_2C_1 \cdot {}_3C_1}{{}_6C_2}$$

$$= \frac{2 + 3 + 6}{15} = \frac{11}{15}$$
26. $P(E') = 1 - P(E) = 1 - p = 1 - 0.36 = 0.64$
28. $P(E') = 1 - P(E) = 1 - \frac{5}{6} = \frac{1}{6}$
30. $P(E) = 1 - P(E') = 1 - p = 1 - 0.84 = 0.16$
32. $P(E) = 1 - P(E') = 1 - \frac{59}{100} = \frac{41}{100}$
34. (a) $0.33(111) = 36.63$ million = 36,630,000
 (b) 0.27
 (c) $0.29 + 0.27 = 0.56$
36. (a) $\frac{34}{100} = 0.34$
 (b) $\frac{45}{100} = 0.45$
 (c) $\frac{23}{100} = 0.23$

$$38. (a) \frac{48 + 56}{128} = \frac{104}{128} = \frac{13}{16}$$

$$(b) \frac{4 + 20}{128} = \frac{24}{128} = \frac{3}{16} \quad \left[\text{Note: } 1 - \frac{13}{16} = \frac{3}{16} \right]$$

$$(c) \frac{4}{128} = \frac{1}{32}$$

$$42. (a) \frac{{}_6C_5}{{}_8C_5} = \frac{6}{56} = \frac{3}{28}$$

$$(b) \frac{{}_6C_4 \cdot {}_2C_1}{{}_8C_5} = \frac{15 \cdot 2}{56} = \frac{15}{28} \quad (c)$$

$$\frac{3}{28} + \frac{15}{28} = \frac{18}{28} = \frac{9}{14}$$

$$46. (a) \frac{{}_8C_2({}_{100}C_5)}{{}_{108}C_7} = 0.0756$$

$$(b) \frac{{}_8C_2({}_{25}C_2)({}_{25}C_3)}{{}_{108}C_7} \approx 6.929 \times 10^{-4}$$

$$50. (a) \frac{{}_{16}C_5}{{}_{20}C_5} = \frac{4368}{15,504} = \frac{91}{323} \approx 0.282 \text{ (5 good units)}$$

$$(b) \frac{{}_{16}C_4 \cdot {}_4C_1}{{}_{20}C_5} = \frac{1820 \cdot 4}{15,504} = \frac{455}{969} \approx 0.470 \text{ (4 good units)}$$

(c) The probability is 1 because there are only 4 defective units.

$$52. (a) P(E E) = \frac{20}{40} \cdot \frac{20}{40} = \frac{1}{4}$$

$$(b) P(E O \text{ or } O E) = 2 \binom{20}{40} \binom{20}{40} = \frac{1}{2}$$

$$(c) P(N_1 < 30, N_2 < 30) = \frac{29}{40} \cdot \frac{29}{40} = \frac{841}{1600}$$

$$(d) P(N_1 N_1) = \frac{40}{40} \cdot \frac{1}{40} = \frac{1}{40}$$

$$56. (a) P(B B B B) = \left(\frac{1}{2}\right)^4 = \frac{1}{16}$$

$$(b) P(B B B B) + P(G G G G) = \left(\frac{1}{2}\right)^4 + \left(\frac{1}{2}\right)^4 = \frac{1}{8}$$

$$(c) P(\text{at least one boy}) = 1 - P(\text{no boys}) \\ = 1 - P(G G G G) = 1 - \frac{1}{16} = \frac{15}{16}$$

$$58. (0.78)^3 = 0.474552$$

$$40. \frac{54}{31 + 54 + 42 + 20 + 47 + 58} = \frac{54}{252} = \frac{3}{14}$$

44. Total ways to insert paychecks: $5! = 120$ ways

5 correct: 1 way

4 correct: not possible

3 correct: 10 ways

2 correct: 20 ways

1 correct: 45 ways

0 correct: 44 ways

$$(a) \frac{45}{120} = \frac{3}{8}$$

$$(b) \frac{45 + 20 + 10 + 1}{120} = \frac{19}{30}$$

$$48. \frac{{}_{13}C_1 \cdot {}_4C_3 \cdot {}_{12}C_1 \cdot {}_4C_2}{{}_{52}C_5} = \frac{13 \cdot 4 \cdot 12 \cdot 6}{2,598,960}$$

$$= \frac{3744}{2,598,960}$$

$$= \frac{6}{4165}$$

$$54. (a) P(A A) = (0.90)^2 = 0.81$$

$$(b) P(N N) = (0.10)^2 = 0.01$$

$$(c) P(A) = 1 - P(N N) = 1 - 0.01 = 0.99$$

60. (a) If the *center* of the coin falls within the circle of radius $d/2$ around a vertex, the coin will cover the vertex.

$$P(\text{coin covers a vertex}) = \frac{\text{Area in which coin may fall so that it covers a vertex}}{\text{Total area}}$$

$$= \frac{n \left[\pi \left(\frac{d}{2} \right)^2 \right]}{nd^2} = \frac{1}{4} \pi$$

(b) Experimental results will vary.

62. False. The first sentence is true, but the second is false. The complement is to roll a number greater than 2, and its probability is $\frac{2}{3}$.

64. If a weather forecast indicates that the probability of rain is 40%, this means the meteorological records indicate that over an extended period of time with similar weather conditions it will rain 40% of the time.

66. $\frac{3}{2x+3} - 4 = \frac{-1}{2x+3}$

$$\frac{4}{2x+3} = 4$$

$$1 = 2x + 3$$

$$2x = -2$$

$$x = -1$$

68. $\frac{2}{x} - \frac{5}{x-2} = \frac{-13}{x^2-2x} = \frac{-13}{x(x-2)}$

$$2(x-2) - 5(x) = -13$$

$$-3x = -9$$

$$x = 3$$

70. $3 - 4 \ln x = 6$

$$4 \ln x = -3$$

$$\ln x = -\frac{3}{4}$$

$$x = e^{-3/4} \approx 0.4724$$

72. $5 \ln 2x - 4 = 11$

$$\ln 2x = 3$$

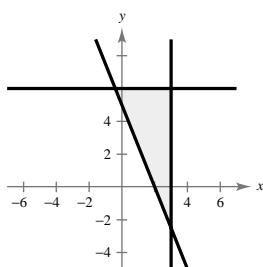
$$2x = e^3$$

$$x = \frac{1}{2} e^3 \approx 10.0428$$

74. $x \leq 3$

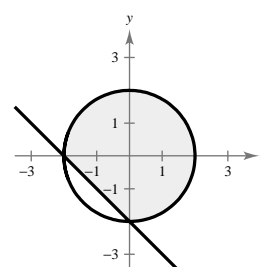
$$y \leq 6$$

$$5x + 2y \geq 10$$



76. $x^2 + y^2 \leq 4$ circle

$$x + y \geq -2$$



78. ${}_9C_5 = 126$

80. ${}_{16}C_{13} = 560$