

## Chapter 10 continued

79. 
$$\begin{aligned} \frac{4}{2x^2} + \frac{1}{3x} &= \frac{4}{2x^2} \left( \frac{3}{3} \right) + \frac{1}{3x} \left( \frac{2x}{2x} \right) \\ &= \frac{12 + 2x}{6x^2} \\ &= \frac{6 + x}{3x^2} \\ &= \frac{x + 6}{3x^2} \end{aligned}$$

80. 
$$\begin{aligned} \frac{11}{4(x-5)} - \frac{x+1}{4x} &= \frac{11x}{4(x-5)x} - \frac{(x+1)(x-5)}{4x(x-5)} \\ &= \frac{11x - [x^2 - 4x - 5]}{4x^2 - 20x} \\ &= \frac{11x - x^2 + 4x + 5}{4x^2 - 20x} \\ &= \frac{-x^2 + 15x + 5}{4x^2 - 20x} \end{aligned}$$

81. 
$$\begin{aligned} \frac{3x}{x^2} - \frac{x-1}{x+3} &= \frac{3x(x+3) - x^2(x-1)}{x^3 + 3x^2} \\ &= \frac{3x^2 + 9x - x^3 + x^2}{x^3 + 3x^2} \\ &= \frac{-x^3 + 4x^2 + 9x}{x^3 + 3x^2} \\ &= \frac{x(-x^2 + 4x + 9)}{x(x^2 + 3x)} \\ &= \frac{-x^2 + 4x + 9}{x^2 + 3x} \end{aligned}$$

82. 
$$\begin{aligned} \frac{2}{3x+2} + \frac{5x^2}{x-4} &= \frac{2}{3x+2} \left( \frac{x-4}{x-4} \right) + \frac{5x^2}{x-4} \left( \frac{3x+2}{3x+2} \right) \\ &= \frac{2x - 8 + 15x^3 + 10x^2}{(3x+2)(x-4)} \\ &= \frac{15x^3 + 10x^2 + 2x - 8}{(3x+2)(x-4)} \end{aligned}$$

83. 
$$\begin{aligned} \frac{1-3x}{x-6} + \frac{2}{2x+1} &= \frac{1-3x}{x-6} \left( \frac{2x+1}{2x+1} \right) + \frac{2}{2x+1} \left( \frac{x-6}{x-6} \right) \\ &= \frac{2x+1 - 6x^2 - 3x + 2x - 12}{(x-6)(2x+1)} \\ &= \frac{-6x^2 + x - 11}{(x-6)(2x+1)} \end{aligned}$$

### Lesson 10.2

#### 10.2 Guided Practice (p. 598)

- focus; directrix
- The graph of  $y = ax^2$  rotated 90° clockwise is the graph of  $x = ay^2$ .

3.  $y = ax^2$

$$x^2 = \frac{1}{a}y$$

$$4p = \frac{1}{a}$$

$$p = \frac{1}{4a}$$

focus:  $\left(0, \frac{1}{4a}\right)$

directrix:  $y = -\frac{1}{4a}$

4.  $x^2 = 4y$

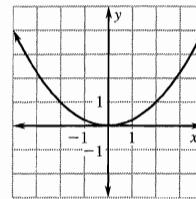
$$4p = 4$$

$$p = 1$$

focus:  $(0, 1)$

directrix:  $y = -1$

$p > 1$  parabola opens up only positive  $y$  values



5.  $y = -5x^2$

$$-\frac{1}{5}y = x^2$$

$$x^2 = -\frac{1}{5}y$$

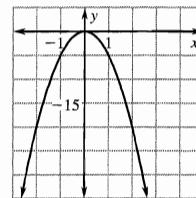
$$4p = -\frac{1}{5}$$

$$p = -\frac{1}{20}$$

focus:  $(0, -\frac{1}{20})$

directrix:  $y = \frac{1}{20}$

$p < 0$  parabola opens down, only negative  $y$ -values



6.  $-12x = y^2$

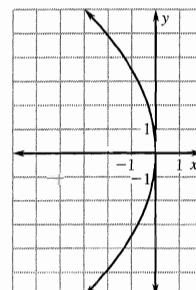
$$4p = -12$$

$$p = -\frac{12}{4} = -3$$

focus:  $(-3, 0)$

directrix is  $x = 3$

$p < 0$  parabola opens left, only negative  $x$ -values



$x$	-1	-2	-3	-4
$y$	$\pm 3.46$	$\pm 4.90$	$\pm 6$	$\pm 6.93$

## Chapter 10 continued

7.  $8y^2 = x$

$$y^2 = \frac{1}{8}x$$

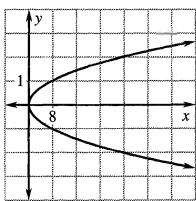
$$4p = \frac{1}{8}$$

$$p = \frac{1}{32}$$

focus:  $(\frac{1}{32}, 0)$

directrix:  $x = -\frac{1}{32}$

$p > 0$  parabola opens right, only positive  $x$ -values



8.  $-6x = y^2$

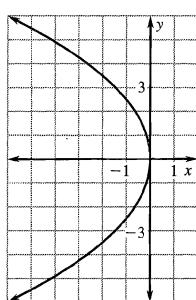
$$4p = -6$$

$$p = -\frac{3}{2}$$

focus:  $(-\frac{3}{2}, 0)$

directrix:  $x = \frac{3}{2}$

$p < 0$  parabola opens left, only negative  $x$ -values



9.  $x^2 = 2y$

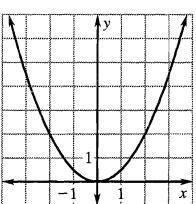
$$4p = 2$$

$$p = \frac{1}{2}$$

focus:  $(0, \frac{1}{2})$

directrix:  $y = -\frac{1}{2}$

$p > 0$  parabola opens up, only positive  $y$ -values



10. focus:  $(0, 3)$

focus:  $(0, p); x^2, p = 3$

directrix:  $y = -p = -3$

$$x^2 = 4py$$

$$x^2 = 4(3)y$$

$$x^2 = 12y$$

12. focus:  $(-6, 0)$

focus:  $(p, 0); y^2, p = -6$

directrix:  $x = -p = 6$

$$y^2 = 4px$$

$$y^2 = 4(-6)x$$

$$y^2 = -24x$$

11. focus:  $(5, 0)$

focus:  $(p, 0); y^2, p = 5$

directrix:  $x = -p = -5$

$$y^2 = 4px$$

$$y^2 = 4(5)x$$

$$y^2 = 20x$$

13. directrix:  $x = 4$ ,

$x = -p$ ,

$p = -4$

focus:  $(4, 0)$

$$y^2 = 4px$$

$$y^2 = 4(-4)x$$

$$y^2 = -16x$$

14. directrix:  $x = -1$ ,

$$x = -p, p = 1$$

focus:  $(1, 0)$

$$y^2 = 4px$$

$$y^2 = 4(1)x$$

$$y^2 = 4x$$

15. directrix:  $y = 8$ ,

$$y = -p, p = -8$$

focus:  $(0, -8)$

$$x^2 = 4py$$

$$x^2 = 4(-8)y$$

$$x^2 = -32y$$

### 10.2 Practice and Applications (pp. 598–600)

16.  $y^2 = 4x$  D    17.  $x^2 = -4y$  B    18.  $x^2 = 4y$  A

19.  $y^2 = -4x$  E    20.  $y^2 = \frac{1}{4}x$  F    21.  $x^2 = \frac{1}{4}y$  C

22.  $y = -3x^2$

$$-\frac{1}{3}y = x^2$$

$$-\frac{1}{3} = 4p$$

$$-\frac{1}{12} = p$$

$p < 0$  parabola opens down

23.  $-9x^2 = 2y$

$$x^2 = -\frac{2}{9}y$$

$$4p = -\frac{2}{9}$$

$$p = -\frac{2}{9}(\frac{1}{4})$$

$$= -\frac{2}{36} = -\frac{1}{18}$$

$p < 0$  parabola opens down

24.  $2y^2 = -6x$

$$y^2 = -3x$$

$$4p = -3$$

$$p = -\frac{3}{4}$$

$p < 0$  parabola opens left

25.  $x = 7y^2$

$$\frac{1}{7}x = y^2$$

$$\frac{1}{7} = 4p$$

$$\frac{1}{28} = p$$

$p > 0$  parabola opens right

26.  $x^2 = 16y$

$$4p = 16$$

$$p = 4$$

$p > 0$  parabola opens up

27.  $-3y^2 = 8x$

$$y^2 = -\frac{8}{3}x$$

$$4p = -\frac{8}{3}$$

$$p = -\frac{8}{12} = -\frac{2}{3}$$

$p < 0$  parabola opens left

28.  $-5x = -y^2$

$$5x = y^2$$

$$5 = 4p$$

$$\frac{5}{4} = p$$

$p > 0$  parabola opens right

29.  $x^2 = \frac{4}{3}y$

$$4p = \frac{4}{3}$$

$$p = \frac{4}{12} = \frac{1}{3}$$

$p > 0$  parabola opens up

30.  $3x^2 = -y$

$$x^2 = -\frac{1}{3}y$$

$$4p = -\frac{1}{3}$$

$$p = -\frac{1}{12}$$

focus:  $(0, -\frac{1}{12})$

directrix:  $y = \frac{1}{12}$

31.  $2y^2 = x$

$$y^2 = \frac{1}{2}x$$

$$4p = \frac{1}{2}$$

$$p = \frac{1}{8}$$

focus:  $(\frac{1}{8}, 0)$

directrix:  $x = -\frac{1}{8}$

## Chapter 10 continued

2.  $x^2 = 8y$

$$-\frac{1}{p} = 8$$

$$p = -\frac{1}{8}$$

focus:  $(0, 2)$

directrix:  $y = -2$

4.  $\frac{x^2}{16} = -16x$

$$-\frac{1}{p} = -16$$

$$p = -\frac{1}{16}$$

focus:  $(-4, 0)$

directrix:  $x = 4$

6.  $-4x + 9y^2 = 0$

$$9y^2 = 4x$$

$$y^2 = \frac{4}{9}x$$

$$4p = \frac{4}{9}$$

$$p = \frac{4}{36} = \frac{1}{9}$$

focus:  $(\frac{1}{9}, 0)$

directrix:  $x = -\frac{1}{9}$

8.  $x = 12x$

$$-\frac{1}{p} = 12$$

$$p = -\frac{1}{12}$$

focus:  $(3, 0)$

directrix:  $x = -3$

10. parabola opens right, only positive  $x$ -values

$x$	1	2	3	4
	$\pm 3.46$	$\pm 4.90$	$\pm 6$	$\pm 6.9$

12.  $y = -6y$

$$-\frac{1}{p} = -6$$

$$p = -\frac{1}{6}$$

focus:  $(0, -\frac{3}{2})$

directrix:  $y = \frac{3}{2}$

14. parabola opens down, only negative  $y$ -values

$x$	-1	-2	-3	-4	-5
	-2.45	$\pm 3.46$	$\pm 4.24$	$\pm 4.9$	$\pm 5.48$

16.  $x = -2x$

$$-\frac{1}{p} = -2$$

$$p = -\frac{1}{2}$$

focus:  $(-\frac{1}{2}, 0)$

directrix:  $x = \frac{1}{2}$

18. parabola opens left, only negative  $x$ -values

$x$	-1	-2	-3	-4	-5
	-1.41	2	$\pm 2.45$	$\pm 2.83$	$\pm 3.16$

33.  $y^2 = -10x$

$$4p = -10$$

$$p = -\frac{10}{4} = -\frac{5}{2}$$

focus:  $(-\frac{5}{2}, 0)$

directrix:  $x = \frac{5}{2}$

35.  $x^2 = -36y$

$$4p = -36$$

$$p = -9$$

focus:  $(0, -9)$

directrix:  $y = 9$

37.  $-28y + x^2 = 0$

$$x^2 = 28y$$

$$4p = 28$$

$$p = 7$$

focus:  $(0, 7)$

directrix:  $y = -7$

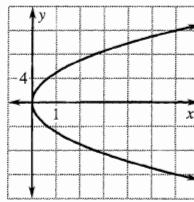
41.  $y^2 = 24x$

$$4p = 24$$

$$p = 6$$

focus:  $(6, 0)$

directrix:  $x = -6$



$p > 0$  parabola opens right, only positive  $x$ -values

$x$	1	2	3	4
	$\pm 4.90$	$\pm 6.93$	$\pm 8.49$	$\pm 9.80$

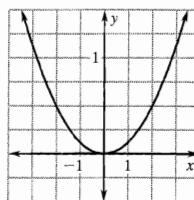
42.  $x^2 = 8y$

$$4p = 8$$

$$p = 2$$

focus:  $(0, 2)$

directrix:  $y = -2$



$p > 0$  parabola opens up, only positive  $y$ -values

$x$	1	2	3
	$\pm 2.83$	$\pm 4$	$\pm 6.90$

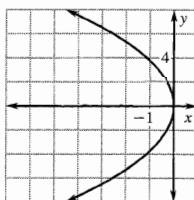
43.  $y^2 = -14x$

$$4p = -14$$

$$p = -\frac{14}{4} = -\frac{7}{2}$$

focus:  $(-\frac{7}{2}, 0)$

directrix:  $x = \frac{7}{2}$



$p < 0$  parabola opens left, only negative  $x$ -values

$x$	-1	-2	-3
	$\pm 3.74$	$\pm 5.29$	$\pm 6.48$

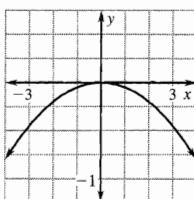
44.  $x^2 = -20y$

$$4p = -20$$

$$p = -5$$

focus:  $(0, -5)$

directrix:  $y = 5$



$p < 0$  parabola opens down, only  $y$ -values

$x$	-1	-2	-3	-4	-5
	$\pm 4.47$	$\pm 6.32$	$\pm 7.75$	$\pm 8.94$	$\pm 10$

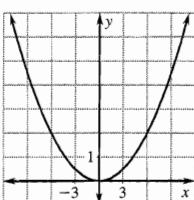
45.  $x^2 = 18y$

$$4p = 18$$

$$p = \frac{18}{4} = \frac{9}{2}$$

focus:  $(0, \frac{9}{2})$

directrix:  $y = -\frac{9}{2}$



$p > 0$  parabola opens up, only  $y$ -values

$x$	1	2	3	4	5
	$\pm 4.24$	$\pm 6$	$\pm 7.35$	$\pm 8.49$	$\pm 9.49$

## Chapter 10 continued

46.  $x^2 = -4y$

$$4p = -4$$

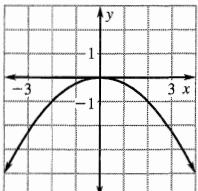
$$p = -1$$

focus:  $(0, -1)$

directrix:  $y = 1$

$p < 0$  parabola opens down, only negative  $y$ -values

$x$	1	2	3
$y$	$\pm 2$	$\pm 2.83$	$\pm 3.46$



47.  $x^2 = 16y$

$$4p = 16$$

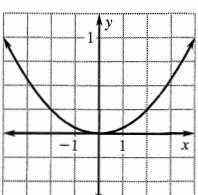
$$p = 4$$

focus:  $(0, 4)$

directrix:  $y = -4$

$p > 0$  parabola opens up, only positive  $y$ -values

$x$	1	2	3	4
$y$	$\pm 4$	$\pm 5.66$	$\pm 6.93$	$\pm 8$



48.  $y^2 = 9x$

$$4p = 9$$

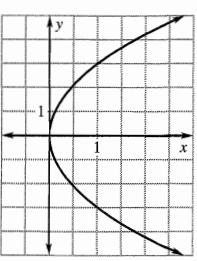
$$p = \frac{9}{4}$$

focus:  $(\frac{9}{4}, 0)$

directrix:  $x = -\frac{9}{4}$

$p > 0$  parabola opens right, only positive  $x$ -values

$x$	1	2	3
$y$	$\pm 3$	$\pm 4.24$	$\pm 5.20$



49.  $y^2 = -3x$

$$4p = -3$$

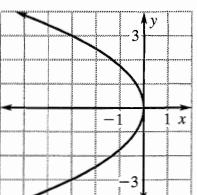
$$p = -\frac{3}{4}$$

focus:  $(-\frac{3}{4}, 0)$

directrix:  $x = \frac{3}{4}$

$p < 0$  parabola opens left, only negative  $x$ -values

$x$	-1	-2	-3
$y$	$\pm 1.73$	$\pm 2.45$	$\pm 3$



50.  $x^2 - 40y = 0$

$$x^2 = 40y$$

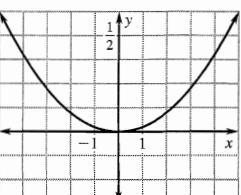
$$4p = 40$$

$$p = 10$$

focus:  $(0, 10)$

directrix:  $y = -10$

$p > 0$  parabola opens up, only positive  $y$  values



$x$	10	20	30	40	50
$y$	$\pm 20$	$\pm 28.28$	$\pm 34.64$	$\pm 40$	$\pm 44.72$

51.  $x + \frac{1}{20}y^2 = 0$

$$\frac{1}{20}y^2 = -x$$

$$y^2 = -20x$$

$$4p = -20$$

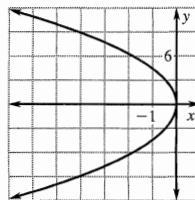
$$p = -5$$

focus:  $(-5, 0)$

directrix:  $x = 5$

$p < 0$  parabola opens left, only negative  $x$ -values

$x$	-1	-2	-3	4
$y$	$\pm 4.47$	$\pm 6.32$	$\pm 7.75$	$\pm 8.94$



52.  $3x^2 = 4y$

$$x^2 = \frac{4}{3}y$$

$$4p = \frac{4}{3}$$

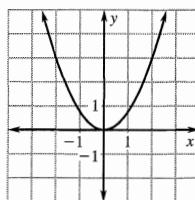
$$p = \frac{1}{12} = \frac{1}{3}$$

focus:  $(0, \frac{1}{3})$

directrix:  $y = -\frac{1}{3}$

$p > 0$  parabola opens up, only positive  $y$ -values

$x$	1	2	3
$y$	$\pm \frac{4}{3}$	$\pm \frac{8}{3}$	$\pm \frac{12}{3} = 4$



53.  $x - \frac{1}{8}y^2 = 0$

$$-\frac{1}{8}y^2 = -x$$

$$y^2 = 8x$$

$$4p = 8$$

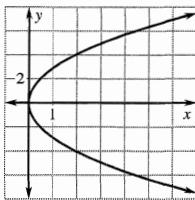
$$p = 2$$

focus:  $(2, 0)$

directrix:  $x = -2$

$p > 0$ , parabola opens to the right, only positive  $x$ -values

$x$	1	2	3
$y$	$\pm 2.83$	4	$\pm 4.90$



54.  $(4, 0) p = 4$

$(-2, 0) p = -2$

$$y^2 = 4px$$

$$y^2 = 4px$$

$$y^2 = 4(4)x$$

$$y^2 = 4(-2)x$$

$$y^2 = 16x$$

$$y^2 = -8x$$

56.  $(-3, 0) p = -3$

$(0, 1) p = 1$

$$y^2 = 4px$$

$$x^2 = 4py$$

$$y^2 = 4(-3)x$$

$$x^2 = 4(1)y$$

$$y^2 = -12x$$

$$x^2 = 4y$$

## Chapter 10 continued

58.  $(0, 4) p = 4$

$$x^2 = 4py$$

$$x^2 = 4(4)y$$

$$x^2 = 16y$$

59.  $(0, -3) p = -3$

$$x^2 = 4py$$

$$x^2 = 4(-3)y$$

$$x^2 = -12y$$

60.  $(0, -4) p = -4$

$$x^2 = 4py$$

$$x^2 = 4(-4)y$$

$$x^2 = -16y$$

62.  $(-\frac{1}{4}, 0) p = -\frac{1}{4}$

$$y^2 = 4px$$

$$y^2 = 4(\frac{1}{4})x$$

$$y^2 = -x$$

64.  $(0, \frac{1}{2}) p = \frac{1}{2}$

$$x^2 = 4py$$

$$x^2 = 4(\frac{1}{2})y$$

$$x^2 = 2y$$

66.  $y = 2 p = -2$

$$x^2 = 4py$$

$$x^2 = 4(-2)y$$

$$x^2 = -8y$$

68.  $x = -4 p = 4$

$$y^2 = 4px$$

$$y^2 = 4(4)x$$

$$y^2 = 16x$$

70.  $x = -5 p = 5$

$$y^2 = 4px$$

$$y^2 = 4(5)x$$

$$y^2 = 20x$$

72.  $x = 2 p = -2$

$$y^2 = 4px$$

$$y^2 = 4(-2)x$$

$$y^2 = -8x$$

74.  $x = -\frac{1}{2} p = \frac{1}{2}$

$$y^2 = 4px$$

$$y^2 = 4(\frac{1}{2})x$$

$$y^2 = 2x$$

76.  $y = \frac{5}{8} p = -\frac{5}{8}$

$$x^2 = 4py$$

$$x^2 = 4(-\frac{5}{8})y$$

$$x^2 = -\frac{5}{2}y$$

59.  $(0, -3) p = -3$

$$x^2 = 4py$$

$$x^2 = 4(-3)y$$

$$x^2 = -12y$$

61.  $(-5, 0) p = -5$

$$y^2 = 4px$$

$$y^2 = 4(-5)x$$

$$y^2 = -20x$$

63.  $(0, -\frac{3}{8}) p = -\frac{3}{8}$

$$x^2 = 4py$$

$$x^2 = 4(-\frac{3}{8})y$$

$$x^2 = -\frac{12}{8}y = -\frac{3}{2}y$$

65.  $(\frac{5}{12}, 0) p = \frac{5}{12}$

$$y^2 = 4px$$

$$y^2 = 4(\frac{5}{12})x$$

$$y^2 = \frac{20}{12}y = \frac{5}{3}x$$

67.  $y = -3 p = 3$

$$x^2 = 4py$$

$$x^2 = 4(3)y$$

$$x^2 = 12y$$

69.  $x = 6 p = -6$

$$y^2 = 4px$$

$$y^2 = 4(-6)x$$

$$y^2 = -24x$$

71.  $y = -1 p = 1$

$$x^2 = 4py$$

$$x^2 = 4(1)y$$

$$x^2 = 4y$$

73.  $y = 4 p = -4$

$$x^2 = 4py$$

$$x^2 = 4(-4)y$$

$$x^2 = -16y$$

75.  $x = \frac{3}{4} p = -\frac{3}{4}$

$$y^2 = 4px$$

$$y^2 = 4(-\frac{3}{4})x$$

$$y^2 = -3x$$

77.  $y = -\frac{1}{12} p = \frac{1}{12}$

$$x^2 = 4py$$

$$x^2 = 4(\frac{1}{12})y$$

$$x^2 = \frac{1}{3}y$$

78.  $y = -4 p = 4$

$$x^2 = 4py$$

$$x^2 = 4(4)y$$

$$x^2 = 16y$$

$$(4)^2 = 16y$$

$$16 = 16y$$

$$\frac{16}{16} = y$$

$$y = 1 \text{ ft}$$

79.

$$x = -1.5$$

$$y^2 = 4px$$

$$y^2 = 4(1.5)x$$

$$y^2 = 6x$$

$$(3.5)^2 = 6x$$

$$12.25 = 6x$$

$$2.04 \text{ inches} = x$$

80.  $y^2 = 4px$

81.  $x^2 = 4py$

$$(6)^2 = 4p(4)$$

$$36 = 16p$$

$$\frac{36}{16} = p$$

$$\text{diameter} = 2(16.97)$$

$$2.25 \text{ in.} = p$$

$$\approx 33.94 \text{ inches}$$

82.  $y = ax^2, \frac{1}{a}y = x^2, 4p = \frac{1}{a}, p = \frac{4}{a}$

focus:  $\left(0, \frac{4}{a}\right)$

directrix:  $y = -\frac{4}{a}$

As  $|a|$  increases, focus and directrix move closer to the origin.

83. a.  $y^2 = \frac{32}{7}x$

$$4p = \frac{32}{7}$$

$$p = \frac{32}{28} = \frac{8}{7} = 1\frac{1}{7}$$

$$\text{depth is } 1\frac{1}{2}$$

$$1\frac{1}{7} < 1\frac{1}{2}$$

b.  $y^2 = \frac{16}{7}(3)$

$$y^2 = \frac{48}{7}$$

$$y = 2.62$$

$$2(2.62) \approx$$

$$5.2 \text{ inches}$$

c.  $y^2 = 6x$

$$y^2 = 6(\frac{3}{2})$$

$$y = 2.62$$

$$y = 3$$

$$2(3) =$$

$$6 \text{ inches}$$

If not the bulb would extend outside of the flashlight.

d.  $y^2 = 2x$

$$y^2 = 2(\frac{3}{2})$$

$$y^2 = 3$$

$$y \approx 1.73$$

$$2(1.73) \approx 3.46 \text{ inches}$$

84.  $x^2 = 4py, \text{ focus: } (0, p), \text{ directrix: } y = -p$

$$\sqrt{x^2} = \sqrt{4py}$$

$$x = \sqrt{4py}$$

$$2x = \text{width} = \text{latus rectum} = 2\sqrt{4py}$$

$$2x = 2\sqrt{4py}$$

$$2x = 2(2)\sqrt{py}$$

$$2x = 4\sqrt{p^2}$$

$$2x = 4p$$

## Chapter 10 continued

### 10.2 Mixed Review (p. 600)

85.  $8^{5x} = 16^{2x+1}$

$$(2^3)^{5x} = (2^4)^{2x+1}$$

$$(2)^{15x} = (2)^{8x+4}$$

$$15x = 8x + 4$$

$$7x = 4$$

$$x = \frac{4}{7}$$

87.  $5^x = 7$

$$\log_5 7 = x$$

$$\frac{\log 7}{\log 5} = x$$

$$1.209 \approx x$$

89.  $\log_7(3x - 5) = \log_7 8x$

$$3x - 5 = 8x$$

$$-5 = 5x$$

$$-1 = x$$

no solution

91.  $\frac{3xy^3}{x^3y} \cdot \frac{y}{6x} = \frac{y^3}{2x^3}$

92.  $\frac{3xy^3}{2x} \div \frac{2xy^3}{3x}$

$$\frac{3xy^3}{2x} \cdot \frac{3x}{2xy^3} = \frac{9}{4}$$

93.  $\frac{x^2 - 9}{x^2 - x - 6} \cdot (x + 2) = \frac{(x-3)(x+3)}{(x-3)(x+2)} \cdot \frac{(x+2)}{1}$

$$= x + 3$$

94.  $\frac{-3x}{x+2} + \frac{4x}{x-1} = \frac{-3x(x-1)}{(x+2)(x-1)} + \frac{4x(x+2)}{(x+2)(x-1)}$

$$= \frac{-3x^2 + 3x + 4x^2 + 8x}{(x+2)(x-1)}$$

$$= \frac{x^2 + 11x}{(x+2)(x-1)}$$

95.  $\frac{x+1}{6x^2} - \frac{x+1}{6x^2 + 6x} = \frac{(x+1)\left(1 + \frac{1}{x}\right)}{6x^2\left(1 + \frac{1}{x}\right)} - \frac{x+1}{6x^2 + 6x}$

$$= \frac{x+1 + 1 + \frac{1}{x} - x - 1}{6x^2\left(1 + \frac{1}{x}\right)}$$

$$= \frac{1 + \frac{1}{x}}{6x^2\left(1 + \frac{1}{x}\right)} = \frac{1}{6x^2}$$

86.  $3^x = 15$

$$\log_3 15 = x$$

$$\frac{\log 15}{\log 3} = x$$

$$2.465 \approx x$$

96.  $\frac{x^2 - 3x + 2}{x - 1} - \frac{x^2 - 4}{x - 2}$

$$= \frac{(x^2 - 3x + 2)(x - 2) - (x^2 - 4)(x - 1)}{(x - 1)(x - 2)}$$

$$= \frac{x^3 - 3x^2 + 2x - 2x^2 + 6x - 4 - [x^3 - x^2 - 4x + 4]}{(x - 1)(x - 2)}$$

$$= \frac{x^3 - 3x^2 + 2x - 2x^2 + 6x - 4 - x^3 + x^2 + 4x - 4}{(x - 1)(x - 2)}$$

$$\frac{-4x^2 + 12x - 8}{(x - 1)(x - 2)} = \frac{-4(x^2 - 3x + 2)}{(x - 1)(x - 2)}$$

$$= \frac{-4(x-2)(x-1)}{(x-1)(x-2)} = -4$$

97.  $(3, 4), (6, 7)$

$$d = \sqrt{(6-3)^2 + (7-4)^2} = \sqrt{9+9}$$

$$= \sqrt{18} = \sqrt{9(2)} = 3\sqrt{2} \approx 4.243$$

98.  $(-3, 7), (-7, 3)$

$$d = \sqrt{(-7+3)^2 + (3-7)^2} = \sqrt{16+16}$$

$$= \sqrt{2(16)} = 4\sqrt{2} \approx 5.657$$

99.  $(18, -4), (-2, 9)$

$$d = \sqrt{(-2-18)^2 + (9+4)^2}$$

$$= \sqrt{400+169} = \sqrt{569} \approx 23.854$$

100.  $(3.7, 5.1), (2, 5)$

$$d = \sqrt{(2-3.7)^2 + (5-5.1)^2}$$

$$= \sqrt{2.89+0.01} = \sqrt{2.9} \approx 1.703$$

101.  $(-9, -31), (8, 7)$

$$d = \sqrt{(8+9)^2 + (7+31)^2}$$

$$= \sqrt{289+1444} = \sqrt{1733} \approx 41.629$$

102.  $(8.8, 3.3), (1.2, 6)$

$$d = \sqrt{(1.2-8.8)^2 + (6-3.3)^2}$$

$$= \sqrt{57.76+7.29} = \sqrt{65.05} \approx 8.065$$

103.  $A = 2.25, P = 1.5, \frac{A}{P} = x$

$$\frac{2.25}{1.5} = 1.5, \frac{A}{P} = x, A = xp, A = 1.5p$$

## Lesson 10.3

### 10.3 Guided Practice (p. 604)

- The set of all points  $(x, y)$  equidistant from a fixed point.
- sometimes true
- They are negative reciprocals of each other (except if one line is vertical).
- The student failed to square the radius;  $x^2 + y^2 = 16$